

# A Study of Eight Visual-spectroscopic Southern Binaries Using Recent SOAR **Observations**

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# Abstract

Speckle observations performed between 2019 and 2022 with the HRCam attached to the 4.1 m SOAR telescope (Cerro Pachón, Chile) permitted to improve visual orbits of the southern binaries WDS 01243-0655 (BU 1163), WDS 09275-5806 (CHR 240), WDS 12114-1647 (S 643 AaAb), WDS 13317-0219 (HDS 1895), WDS 15282- 0921 (BAG 25 AaAb), WDS 17304-0104 (STF 2173), WDS 19598-0957 (HO 276), and WDS 21274-0701 (HDS 3053). All of them are spectroscopic binaries, of which six are SB2, so relevant information about their individual masses has been obtained. Moreover, comparison between different values of their parallaxes (orbital, dynamic, and ANAPAR, a color-dependent model suitable for binary systems attending to the exact locations of the components on the MS in the HR diagram) with those provided by Hipparcos and Gaia missions, along with comments for each binary are presented. The luminosity determination of the 16 components allowed us to estimate their approximate age and position on the HR diagram as well.

Unified Astronomy Thesaurus concepts: [Orbit determination](http://astrothesaurus.org/uat/1175) (1175); [Orbits](http://astrothesaurus.org/uat/1184) (1184); [Stellar astronomy](http://astrothesaurus.org/uat/1583) (1583); [Stellar dynamics](http://astrothesaurus.org/uat/1596) (1596); [Stellar evolutionary tracks](http://astrothesaurus.org/uat/1600) (1600); [Stellar masses](http://astrothesaurus.org/uat/1614) (1614); [Stellar parallax](http://astrothesaurus.org/uat/1618) (1618); [Binary](http://astrothesaurus.org/uat/154) [stars](http://astrothesaurus.org/uat/154) (154); [Visual binary stars](http://astrothesaurus.org/uat/1777) (1777); [Spectroscopic binary stars](http://astrothesaurus.org/uat/1557) (1557)

# 1. Introduction

It is well known that double and multiple stars represent a fundamental source of astronomical information, not only because we can determine the masses of the components from their orbits, which in itself is a very important motivation for their study, but also because such stellar systems allow to research multiple physical and dynamical phenomena: Keplerian and perturbed orbits, multiple stellar systems, establishing the mass–luminosity relationship, orbital and dynamical parallaxes, influence of radiation induced mass loss and transference, variable components of different kinds, magnetic binaries, etc.

In the 1970s a new technique for the optical observation and identification of new components appeared. Speckle interferometry (Labeyrie [1970](#page-13-0)) has allowed the obtaining astrometric positions and differential photometry with unprecedented precision. Mainly used in class 4–6 m telescopes, it was at that moment a true revolution in this field of research that reaches our time accompanied by adaptive optics and long baseline interferometry.

By means of speckle interferometry, it is possible to overcome the limits imposed by the atmospheric seeing and achieve resolutions close to the diffraction limit of the telescope. This allowed several groups to resolve optically several spectroscopic binaries (see, for example, McAlister [1976,](#page-13-0) [1977](#page-13-0), [1978](#page-13-0); Balega et al. [1984;](#page-12-0) Barlow et al. [1993](#page-12-0); Pourbaix [1998](#page-13-0)). This fact was specially important for the

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determination of three-dimensional orbits, and therefore the deduction of the orbital parallaxes and the individual masses.

Another quality leap happened twenty years later with the launch of the astrometric satellite, Hipparcos (Perryman et al. [1997;](#page-13-0) van Leeuwen [2007](#page-14-0)). This satellite yielded parallaxes that, in many cases, were vastly superior to those obtained from the ground, which improved the precision of the calculated stellar masses, besides providing many measured parameters, the detection of astrometric orbits, and photometric and astrometric information. Nowadays in the Gaia era (Gaia Collaboration et al. [2016,](#page-13-0) [2018,](#page-13-0) [2023](#page-13-0)) all the astronomical research, and in particular binary stars, have reached a golden age, mainly after the data releases DR2, EDR3, and DR3, and with the prospect of all the information available in the full catalog expected for 2030.

The use of large ground-based telescopes with modern detectors, along with the observational data from the space telescopes enables the future research of double and multiple systems from different points of view. Among the active telescopes for the observation of binaries in the southern hemisphere it is the Southern Astrophysical Research telescope (SOAR). The research included in this article is based on recent observations made with the HRCam attached to this 4.1 m telescope, within the collaboration established between the Universities of Chile and Santiago de Compostela through the Ramón María Aller Astronomical Observatory.

The "Speckle Interferometry at SOAR" series (hereafter, TMH10; Tokovinin et al. [2010a](#page-13-0), [2010b](#page-13-0), [2015](#page-13-0), [2016](#page-13-0), [2018](#page-13-0), [2019,](#page-14-0) [2020,](#page-14-0) [2021](#page-13-0), [2022](#page-13-0); Tokovinin [2012](#page-13-0)) explains the characteristics and results of the different observational Speckle interferometry programs that had been developed during more than a decade and a half in SOAR.

<span id="page-1-0"></span>

| Magintudes and Specular Types        |            |       |                  |                  |                  |                         |
|--------------------------------------|------------|-------|------------------|------------------|------------------|-------------------------|
| Washington Double Star Catalog (WDS) | Magnitudes |       | Spectral types   | References       |                  |                         |
|                                      | А          | B     | Combined         | А                | B                | Spectral Types          |
| 01243-0655                           | 6.59       | 6.98  | F <sub>4</sub> V | F3V              | F <sub>6</sub> V | Abt $(2009)$            |
| 09275-5806                           | 7.65       | 8.33  | G2V              | G0V              | G6.5V            | Houk & Cowley $(1975)$  |
| 12114-1647                           | 7.54       | 8.23  | G6V              | G3V              | G9V              | Gray et al. $(2006)$    |
| 13317-0219                           | 7.65       | 9.48  | G9V              | G5.5V            | K3V              | Frasca et al. $(2009)$  |
| 15282-0921                           | 6.93       | 10.42 | G9V              | G8V              | <b>MOV</b>       | Gray et al. (2003)      |
| 17304-0104                           | 6.06       | 6.10  | G5V              | G4.5V            | G5V              | Sharma et al. $(2020)$  |
| 19598-0957                           | 6.22       | 7.83  | F9V              | F <sub>6</sub> V | G8V              | Gray et al. $(2003)$    |
|                                      |            |       | G2V              | F9.5V            | K1V              | Houk $&$ Swift $(1999)$ |
| 21274-0701                           | 7.97       | 9.14  | G0V              | <b>F8.5V</b>     | G8V              | Houk $&$ Swift $(1999)$ |

Table 1 Magnitudes and Spectral Types

Note. This table concerns the magnitudes and the spectral type of each component of the eight binaries studied. In column 1 the Washington Double Star Catalog (WDS) number appear. Columns 2 and 3 correspond to the apparent magnitudes for the components principal (A) and secondary (B). Columns 4 lists the combined spectrum, columns 5 and 6 includes the calculated individual spectral types for the components A and B, respectively, and column 7 the reference for the combined spectrum.

Those campaigns had been developed using the HRCam (Tokovinin & Cantarutti [2008](#page-13-0)) working at the 4.1 m SOAR telescope (Sebring et al. [2003](#page-13-0)). Information regarding the reduction of the data blocks and the astrometrical and photometrical resolution of the systems observed can be obtained in Tokovinin ([2018a](#page-13-0)) and references therein. The nominal diffraction-limited resolution, i.e., the diffraction limit  $\frac{\lambda}{2}$ , is 27 mas at 540 nm wavelength and 40 mas at 800 nm. Standard magnitude limit is  $I \approx 12$  mag under typical seeing, although pairs as faint as I  $\approx$  16 mag can be measured under exceptionally good seeing but with less accuracy and resolution.

We present a study of eight visual binaries, which were tracked by means of speckle interferometry, and that also have a spectroscopic orbit, six of them SB2. Seven of this orbits were obtained from the 9th Catalogue of Spectroscopic Binary Orbits<sup>4</sup> and one from the Gaia Archive (the DR3 two body orbit catalog). Apart from a fine-tuned improvement of their visual orbits shown in the lower rms in  $\theta$  and  $\rho$ , we describe thoroughly the determination of the individual masses of each component and the different parallaxes, comparing our results with those previously deduced by other authors for the same objects.

In order to perform the orbit calculation, in the last decades different methods (Thiele-Innes-Van den Bos, Zwiers, Kowalsky, in Zwiers [1896](#page-14-0); Vidal [1953](#page-14-0); Cid [1958,](#page-12-0) [1960](#page-12-0); Heintz [1978;](#page-13-0) Docobo [1985,](#page-13-0) [2012;](#page-13-0) Catovic & Olevic [1992](#page-12-0); Olević & Cvetković [2004](#page-13-0)), and new optimization techniques to minimize the residuals between observed and calculated positions have been used (Monet [1979;](#page-13-0) Hartkopf et al. [1989](#page-13-0); Wales & Doye [1997;](#page-14-0) Pourbaix [1998](#page-13-0); MacKnight & Horch [2004](#page-13-0); Branham [2005;](#page-12-0) Tokovinin [2016a](#page-13-0); Mendez et al. [2017,](#page-13-0) among others). On our behalf, we have tried not only that the rms in  $\theta$ ,  $\rho$ , and even the radial velocities are minimal, but also that the sequence of signs of the residuals is well distributed, avoiding systematic errors. In this sense, we have used the analytical method of Docobo (Docobo [1985](#page-13-0), [2012](#page-13-0)) in order to calculate a preliminary solution which is later improved by a least squares minimization. Finally, if it is necessary, the method of Docobo is applied again for a final adjustment to avoid systematical deviations, even if they are

small. Logically, a previous step consists in assigning a weight to each observation depending on the technique and the telescope utilized. The scheme for the micrometric observations can be seen in Docobo  $& Ling (2003)$  $& Ling (2003)$  $& Ling (2003)$ ; whereas, for the interferometric observations, the weights are assigned according to the aperture of the telescope because the size of the pixel in the speckle cameras decreases when the aperture increases, therefore improving the resolution: 5 for apertures smaller than 1 m, 10 for 1–2 m, 15 for 2–3 m, 20 for 3–4 m, 25 for 4–5 m, 30 for 5–6 m, and 35 for larger apertures.

As it is well known, the method of Docobo, based on the obtaining of a set of relative orbits that apparent orbits pass through three selected points, without the need for the calculation of the areal constant, permits to choose the best orbit according to different criteria, not only the minimal rms, but also the proximity of the dynamical parallax for each of the orbits, calculated using both the classical Baize–Romani algorithm (Baize & Romani [1946;](#page-12-0) herein designated as dynamical) and the ANAPAR procedure (Andrade [2019](#page-12-0)), to those from Hipparcos and Gaia. Another criterion may be the comparison of the individual masses deduced from the dynamical and ANAPAR parallaxes with the typical masses that correspond to the spectral types of the components.

The individual spectral types were determined by means of the method of Edwards (Edwards [1976;](#page-13-0) Campo [2019](#page-12-0)) from the combined spectrum and the magnitude difference between the components,  $\Delta m$ . The first were taken from Houk & Cowley ([1975](#page-13-0)), Houk & Swift ([1999](#page-13-0)), Gray et al. ([2003](#page-13-0), [2006](#page-13-0)), Abt ([2009](#page-12-0)), Frasca et al. ([2009](#page-13-0)), and Sharma et al. ([2020;](#page-13-0) see Table 1); whereas, for  $\Delta m$ , unless the individual magnitudes are available, we took the mean of the values in the V band from the speckle results of each binary.

Another useful tool that we have used in the present research, is the algorithm to obtain the three-dimensional orbit of a spectroscopic binary with one speckle measurement and the parallax (Docobo et al. [2014](#page-13-0)). This algorithm also permits to study the coherence of the available speckle measurements in each case. We will refer to it in the text as the 3D methodology.

After this introduction, in Section [2](#page-2-0) the results and the comments for each binary are presented.

In Section [3](#page-10-0) we have calculated the absolute magnitudes and luminosities (see Table [8](#page-10-0)) with the aim of determining the position of the different objects in the HR diagram and plotting

https://[sb9.astro.ulb.ac.be](https://sb9.astro.ulb.ac.be/)/

<span id="page-2-0"></span>

Figure 1. Flowchart of the calculation process.

the isochrones with MIST (Paxton et al. [2011](#page-13-0), [2013](#page-13-0), [2015](#page-13-0); Choi et al. [2016](#page-12-0); Dotter [2016](#page-13-0)). The parallaxes that we used have been the ANAPAR parallaxes.

Seven of the orbits studied had been announced in the IAUDS Circular No 207 (Docobo et al. [2022](#page-13-0)), and that of the system BU 1163 in No 209 (Docobo et al. [2023](#page-13-0)).

# 2. Results and Discussion

In Figure 1 a flowchart of the methodology used to obtain the results is presented. We calculate a visual orbit from all the visual and interferometric measurements available, checking their compatibility with the published spectroscopic orbits and the rms error of the difference between the observations and the calculated positions. At the same time, using the combined spectrum and the magnitude difference, we apply the Edwards process to obtain the individual spectra, which in turn provide the standard masses of the components through calibrations such as the one in Pecaut & Mamajek  $(2013)$  $(2013)$  $(2013)$ . This masses represent an additional check for the fitness of the orbit. The visual orbit, along with the spectral decomposition and the magnitudes are used to calculate the dynamical and ANAPAR parallaxes, and for stars with SB2 orbits, we can calculate the orbital parallax from  $a''$ , and  $a$  in astronomical units, which in turn can be determined by using *a* sin *I* from the spectroscopic orbit and I from the visual orbit. The different parallaxes, combined with the visual orbit, by means of Kepler's Third

<span id="page-3-0"></span>

Table 2 Orbital Elements of the Visual Orbits

Note. We Identified in the first column each binary by its WDS number and by the discoverer code, which is the name of the binary, and the corresponding orbital elements with their standard errors (Columns 2–8): the period, P, in years; the time of the periastron passage, T, in Besselian years; the eccentricity, e; the semimajor axis, a, in arcseconds; the inclination, I; the angle of the node,  $\Omega$ ; and the argument of the periastron,  $\omega$ , the last three in degrees. The periastron passage, T, expressed in Julian years and the date of the last observation used in the calculation of the orbit are included in column 9. Previously to the calculation of the orbits, the observations were corrected for precession in order to refer the position angles to the standard equinox of J2000.0.

HDS 3053  $\pm 0.300$   $\pm 0.250$   $\pm 0.005$   $\pm 0.0020$   $\pm 1.0$   $\pm 1.0$   $\pm 1.0$  2020.8339



Table 3 Rms Quality Controls Compared to the Previous Orbits

Notes. In the present table, the weighted rms of the differences between the observed and the calculated values of the  $\theta$  and  $\rho$  coordinates to compare the orbits that we calculate with the last determined are shown. Columns 1 and 2 identify the binary by its WDS number and the name of the binary. Columns 3 and 4 list the rms in  $\theta$ and  $\rho$  obtains with the orbits presented in this paper, and columns 5 and 6 the same rms now deduced using the last orbit, which were calculated by the authors listed in column 7.

<sup>a</sup> We list only the last orbit.

Law, give the sum of the masses of the components, and even the individual masses in the case of the dynamical and ANAPAR parallaxes. For the SB2, the mass sum and the mass ratio yield the individual masses, and for the SB1 we can obtain them from the mass sum, the mass function from the spectroscopic orbit, and the inclination from the visual orbit.

All the information regarding the orbital elements, ephemeris, quality controls of the orbits, parallaxes and masses is included in Tables [1](#page-1-0)–[6](#page-6-0). The values of the parallaxes are also represented in Figure [2](#page-5-0). Figures [3](#page-6-0)–[10](#page-7-0) show the apparent orbits as well as the available observations. The details of the figures can be seen in the caption of Figure [3.](#page-6-0)

# 2.1. WDS 01243-0655 (BU 1163, HIP 6564, HD 8556)

This binary was discovered by S. W. Burnham in 1890 (Aitken & Doolittle [1932](#page-12-0)), and both its components have similar brightness and color, as evidenced by their magnitude difference and spectral types.

Table 4 Orbital Elements of the Spectroscopic Orbits (Only the Last Orbit)

<span id="page-4-0"></span>

| <b>WDS</b>                    | $P$ (day)           | T(RJD)               | $\epsilon$             | $\omega_1(^\circ)$   | $K_1$ (km s <sup>-1</sup> ) | $K_2$ (km s <sup>-1</sup> ) | $\gamma$ (km s <sup>-1</sup> ) | Reference |
|-------------------------------|---------------------|----------------------|------------------------|----------------------|-----------------------------|-----------------------------|--------------------------------|-----------|
| name                          | $\sigma$            | $\sigma$             | $\sigma$               | $\sigma$             | $\sigma$                    | $\sigma$                    | $\sigma$                       |           |
| 01243-0655<br><b>BU 1163</b>  | 5895.01             | 41588.76             | 0.92                   | 0.0                  | 40.1 <sup>a</sup>           |                             |                                | (1)       |
| 09275-5806<br><b>CHR 240</b>  | 513.675<br>± 0.694  | 57171.455<br>± 1.679 | 0.3966<br>$\pm 0.0116$ | 327.53<br>$\pm$ 4.96 | 3.020<br>± 0.146            |                             | 10.486<br>$\pm 0.074$          | (2)       |
| 12114-1647                    | 211.585             | 58383.709            | 0.281                  | 284.0                | 15.484                      | 17.706                      | 2.369                          | (3)       |
| $S$ 634 AaAb                  | $\pm 0.029$         | $\pm$ 0.270          | $\pm 0.002$            | $\pm 0.5$            | $\pm 0.039$                 | $\pm 0.039$                 | $\pm 0.020$                    |           |
| 13317-0219<br><b>HDS 1895</b> | 1188.0<br>$\pm 9.0$ | 49474.8<br>± 5.6     | 0.641<br>$\pm 0.027$   | 355.8<br>± 3.9       | 3.14<br>$\pm 0.16$          |                             | $-51.148$<br>$\pm 0.072$       | (4)       |
| 15282-0921                    | 889.813             | 47967.519            | 0.9733                 | 252.64               | 36.42                       | 52.90                       | 7.47                           | (5)       |
| BAG 25 AaAb                   | $\pm 0.017$         | $\pm 0.015$          | $\pm 0.0006$           | $\pm 0.73$           | $\pm 0.38$                  | $\pm 1.73$                  | $\pm 0.20$                     |           |
| 17304-0104                    | 16924.4             | 37897.97             | 0.1678                 | 328.7                | 4.94                        | 5.32                        | $-77.181$                      | (6)       |
| STF 2173                      | ± 7.7               | ± 56.68              | ± 0.0025               | $\pm 1.3$            | $\pm 0.11$                  | $\pm 0.12$                  | ± 0.069                        |           |
| 19598-0957                    | 1786.27             | 45259.4              | 0.5927                 | 319.8                | 4.69                        | 4.64                        | 29.683                         | (7)       |
| HO 276                        | $\pm 1.68$          | ± 7.1                | $\pm 0.0058$           | ± 2.9                | $\pm$ 0.13                  | $\pm 0.28$                  | ± 0.076                        |           |
| 21274-0701                    | 7576                | 57262.8              | 0.363                  | 324.4                | 3.34                        | 8.66                        | $-0.75$                        | (8)       |
| <b>HDS 3053</b>               | ±14                 | ± 9.8                | $\pm 0.003$            | $\pm 0.7$            | $\pm$ 0.15                  | $\pm 0.14$                  | $\pm 0.14$                     |           |

Notes. The orbital elements of the spectroscopic orbits that had been calculated for the eight binaries studied in this research are included in this table. In order to simplify the information, only the last orbit has been included. In this table, column 1 includes the identifications of each binary in the same mode as the previous tables, that is to say, the WDS number and the name of the binary star. Columns 2–8 give information of the orbital elements of each spectroscopy binary with the corresponding standard errors: the period, P, in days; the periastron passage, T, in reduced Julian days; the eccentricity, the argument of the periastron of the primary,  $\omega_1$  ( $|\omega_1 - \omega| = 180^\circ$ ); the RV amplitude of the primary; the RV amplitude of the secondary; and the velocity of the center of masses. Column 9 provides the reference of each spectroscopic orbit.

<sup>a</sup> Although this is an SB2 system, the authors give  $K_1 + K_2$ .

References. (1) Fletcher ([1973](#page-13-0)), (2) Gaia Collaboration et al. ([2016](#page-13-0), [2023](#page-13-0)), (3) Tokovinin ([2019](#page-13-0)), (4) Latham et al. ([2002](#page-13-0)), (5) Halbwachs et al. ([2018](#page-13-0)), (6) Pourbaix ([2000](#page-13-0)), (7) Pourbaix ([2000](#page-13-0)), (8) Tokovinin ([2018b](#page-13-0)).

The first orbits as a visual binary were calculated by W. H. Van den Bos (van den Bos [1934](#page-14-0)), but by then it was not clear if the orbital period was close to 16 yr or double than that. In the first case it would be a very eccentric orbit, whereas in the second it would be nearly circular. New orbits were obtained later by the same author, in 1956 for both possible periods, and in 1962 for 16 yr (van den Bos [1956,](#page-14-0) [1962](#page-14-0)).

In 1973, Fletcher ([1973](#page-13-0)) determined the first (SB2) spectroscopic orbit using 12 measurements of radial velocities obtained by himself and other authors. Previous spectroscopic observations reported by Evans ([1957](#page-13-0)) and Ishida ([1966](#page-13-0)) did not show enough duplicity of the spectral lines. This orbit showed that the real solution was the one with short period.

New orbits were calculated later by several authors based only on visual measurements (Finsen [1973;](#page-13-0) Morbey [1975](#page-13-0); Starikova [1978](#page-13-0); Hartkopf et al. [1996](#page-13-0); Söderhjelm [1999](#page-13-0)), which improved the previous orbits but now show large errors for the newer observations.

Since the 1970s, this binary has been followed by means of speckle interferometry, mainly by H. A. McAlister (McAlister & Degioia [1979;](#page-13-0) McAlister & Fekel [1980](#page-13-0); McAlister & Hendry [1982](#page-13-0); McAlister et al. [1983;](#page-13-0) McAlister & Hartkopf [1984](#page-13-0); McAlister et al. [1987;](#page-13-0) Al-Shukri et al. [1996](#page-12-0); Fu et al. [1997](#page-13-0)), W. Hartkopf (Hartkopf et al. [1992](#page-13-0), [1993](#page-13-0), [1996](#page-13-0), [1997](#page-13-0), [2000](#page-13-0)), B. D. Mason (Mason et al. [1999;](#page-13-0) Douglass et al. [2000;](#page-13-0) Mason et al. [2001a](#page-13-0), [2001b,](#page-13-0) [2002,](#page-13-0) [2009](#page-13-0)), E. Horch (Horch et al. [1999,](#page-13-0) [2000](#page-13-0), [2001a,](#page-13-0) [2001b,](#page-13-0) [2002,](#page-13-0) [2004](#page-13-0), [2006a,](#page-13-0) [2006b;](#page-13-0) Davidson &

Baptista [2009](#page-12-0); Horch et al. [2011](#page-13-0)), and A. Tokovinin (Tokovinin [1982](#page-14-0), [1983,](#page-14-0) [1985](#page-14-0); Tokovinin & Ismailov [1988;](#page-14-0) Tokovinin et al. [2010a,](#page-13-0) [2010b;](#page-13-0) Hartkopf et al. [2012;](#page-13-0) Tokovinin et al. [2015](#page-13-0)), which has allowed to obtain increasingly accurate orbits. Our visual solution is based on the last measurements carried out by Tokovinin et al. ([2020](#page-14-0)) at SOAR. A comparative between the rms in  $\theta$  and  $\rho$  of the last orbits can be seen in Table [3.](#page-3-0)

Taking into account the spectroscopic orbit by Fletcher (with *a* sin *I* deduced from  $K_1 + K_2$ , and using the values of  $a =$  $0''1996 \pm 0.0010$  and  $I = 117^{\circ}0 \pm 0.5$  from our orbit), we determine an orbital parallax of  $0''02088 \pm 0.0010$  that yields individual masses of 1.70  $\pm$  0.13  $\mathcal{M}_{\odot}$  for each component.

We suggest to perform more radial velocity observations with the aim of determining a more robust spectroscopic orbit, which can be used to deduce an orbital parallax closer to the other parallaxes presented in this work. Our parallax gives individual masses of 1.422 and 1.296  $M_{\odot}$ , which are more in accordance with the spectral types F3V and F6V that we have obtained from the combined spectrum F4V (see Table [1](#page-1-0)). Gaia did not report a parallax for this binary.

# 2.2. WDS 09275-5806 (CHR 240, HIP 46388, HD 82082)

The binary nature of this star was discovered by B. Mason in 1996, and it has been followed by A. Tokovinin by means of speckle interferometry in regular observation campaigns since

<span id="page-5-0"></span>

2010 (Hartkopf et al. [2012](#page-13-0); Tokovinin [2012;](#page-13-0) Tokovinin et al. [2014,](#page-13-0) [2015,](#page-13-0) [2016](#page-13-0), [2020](#page-14-0)).

Despite its very short period ( $\approx$ 1.41 yr), there were only two visual orbits determined by A. Tokovinin (Tokovinin et al. [2015;](#page-13-0) Tokovinin [2016b](#page-13-0)), and an astrometric and an astrospectroscopic orbit reported by Gaia (Gaia Collaboration et al. [2016,](#page-13-0) [2023](#page-13-0)). Both of Gaia's orbits are quite similar with respect to the common elements, but there may be an imprecision in the  $C$  and  $H$  spectroscopic elements, as we will see.

The parallaxes of Hipparcos (0″01997), Gaia (0″01980), and dynamical and ANAPAR (0″02058 and 0″02053) obtained from our orbit, produce mass sums that are in reasonable agreement (between 2.41 and 2.15; see Table [6](#page-6-0)).

However, when we make an estimation of the parallax using the data from the astro-spectroscopic orbit by Gaia, we obtain values that are not suitable. Be it starting from a combined spectrum of G2V (Houk & Cowley [1975](#page-13-0)) or G0V (Cannon & Pickering [1993](#page-12-0)), a  $\Delta m$  of 0.68 (from the speckle measurements) or of 1.2 (from the 6th Catalog of Orbits of Visual Binary Stars (ORB6); Hartkopf et al. [2001a](#page-13-0)), the individual masses should be within a range of  $1.18-1.06$  for  $M_A$  and 0.99-0.94 for  $M_B$ , and with the value of  $a_1$  sin *I* given by Gaia, we reach a linear value of the semimajor axis of the relative orbit,  $a$ , within 0''418–0''390. The resulting parallax calculated as  $\frac{a''}{a} \approx 0''083$  is very different of the rest of the parallaxes; therefore it suggests that, such as we said earlier, it is quite possible that any of the parameters  $C, H$ , or both, have an inadmissible error despite the small uncertainties reported.

## 2.3. WDS 12114-1647 (S 634 AaAb, HIP 59426, HD 105913)

The A component of the stellar system S 634 (of which three stars were known until recently) is an SB2, which spectroscopic orbit was calculated by Tokovinin ([2019](#page-13-0)) with a period close to seven months (see Table [4](#page-4-0)). Therefore, in the three-year interval in which A. Tokovinin obtained five speckle measurements at SOAR (resolved for the first time in 2018), the pair AaAb has

Table 5 Parallaxes (in Arcseconds)

| <b>WDS</b><br>Name    | Orbital<br>$\sigma$ | Hipparcos<br>σ | Gaia<br>$\sigma$ | Dynamical<br>$\sigma$ | ANAPAR<br>$\sigma$ |
|-----------------------|---------------------|----------------|------------------|-----------------------|--------------------|
| 01243-0655            | 0.02088             | 0.02144        |                  | 0.02248               | 0.02283            |
| <b>BU 1163</b>        | 0.00010             | 0.00061        |                  | 0.00029               | 0.00028            |
| 09275-5806            |                     | 0.01997        | 0.01980          | 0.02058               | 0.02053            |
| <b>CHR 240</b>        |                     | 0.00052        | 0.00019          | 0.00009               | 0.00009            |
| 12114-1647            | 0.02676             | 0.03092        | 0.02831          | 0.03103               | 0.03055            |
| S 634 AaAb            | 0.00103             | 0.00095        | 0.00029          | 0.00145               | 0.00136            |
| 13317-0219            |                     | 0.03257        | 0.03776          | 0.03896               | 0.03782            |
| <b>HDS 1895</b>       |                     | 0.00201        | 0.00063          | 0.00074               | 0.00068            |
| 15282-0921            | 0.05184             | 0.04858        | 0.05114          | 0.05333               | 0.05142            |
| <b>BAG</b><br>25 AaAb | 0.00165             | 0.00133        | 0.00074          | 0.00155               | 0.00144            |
| 17304-0104            | 0.06071             | 0.06119        | 0.05960          | 0.06003               | 0.05962            |
| <b>STF 2173</b>       | 0.00097             | 0.00068        | 0.00071          | 0.00173               | 0.00151            |
| 19598-0957            | 0.03664             | 0.04504        | 0.04693          | 0.04275               | 0.04237            |
| HO 276                | 0.00123             | 0.00099        | 0.00093          | 0.00014               | 0.00013            |
| 21274-0701            | 0.01624             | 0.01748        | 0.01549          | 0.01712               | 0.01701            |
| <b>HDS 3053</b>       | 0.00035             | 0.00102        | 0.00040          | 0.00033               | 0.00031            |

Note. The different values of the parallaxes expressed in arcseconds figure in this table. The format is the following: once again the first column inform about the identifications of each binary. Columns 2–6 give the values of the different parallaxes (Orbital, Hipparcos, Gaia, Dynamical, and ANAPAR) with their standard errors.

completed more than five revolutions. The current component B is far from the components AaAb (5″), and for this reason its influence on the close binary is hardly detectable.

Table 6 The Individual Masses (in  $\mathcal{M}_{\odot}$ ), With their Standard Errors, Calculated with the Different Parallaxes

<span id="page-6-0"></span>

|                    |                             | Orbital                     |                             | Hipparcos                   |                             | Gaia                        |                             | Dynamical                   |                             | <b>ANAPAR</b>               |
|--------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| <b>WDS</b><br>Name | $\mathcal{M}_A$<br>$\sigma$ | $\mathcal{M}_B$<br>$\sigma$ |
| 01243-0655         | 1.695                       | 1.695                       | 1.567                       | 1.567                       |                             |                             | 1.422                       | 1.296                       | 1.348                       | 1.249                       |
| <b>BU 1163</b>     | 0.059                       | 0.059                       | 0.143                       | 0.143                       |                             |                             | 0.036                       | 0.033                       | 0.007                       | 0.007                       |
| 09275-5806         |                             |                             | 2.108                       | 0.245                       | 2.165                       | 0.249                       | 1.159                       | 0.991                       | 1.151                       | 1.015                       |
| <b>CHR 240</b>     |                             |                             | 0.598                       | 0.569                       | 0.583                       | 0.578                       | 0.009                       | 0.007                       | 0.002                       | 0.002                       |
| 12114-1647         | 1.475                       | 1.290                       | 0.956                       | 0.836                       | 1.246                       | 1.090                       | 0.960                       | 0.814                       | 0.990                       | 0.869                       |
| S 634 AaAb         | 0.240                       | 0.210                       | 0.141                       | 0.123                       | 0.148                       | 0.130                       | 0.058                       | 0.049                       | 0.019                       | 0.017                       |
| 13317-0219         |                             |                             | 1.873                       | 0.636                       | 1.137                       | 0.473                       | 0.830                       | 0.636                       | 0.886                       | 0.716                       |
| <b>HDS 1895</b>    |                             |                             | 0.487                       | 0.089                       | 0.116                       | 0.036                       | 0.021                       | 0.016                       | 0.007                       | 0.006                       |
| 15282-0921         | 0.834                       | 0.574                       | 1.013                       | 0.698                       | 0.869                       | 0.598                       | 0.842                       | 0.451                       | 0.897                       | 0.546                       |
| BAG 25 AaAb        | 0.101                       | 0.070                       | 0.113                       | 0.077                       | 0.075                       | 0.052                       | 0.032                       | 0.017                       | 0.011                       | 0.007                       |
| 17304-0104         | 0.971                       | 0.901                       | 0.948                       | 0.880                       | 1.026                       | 0.953                       | 0.973                       | 0.964                       | 0.992                       | 0.985                       |
| STF 2173           | 0.080                       | 0.074                       | 0.071                       | 0.066                       | 0.078                       | 0.072                       | 0.042                       | 0.041                       | 0.011                       | 0.011                       |
| 19598-0957         | 1.491                       | 1.507                       | 0.803                       | 0.811                       | 0.710                       | 0.717                       | 1.113                       | 0.775                       | 1.108                       | 0.831                       |
| HO 276             | 0.159                       | 0.160                       | 0.060                       | 0.060                       | 0.049                       | 0.049                       | 0.005                       | 0.003                       | 0.002                       | 0.001                       |
| 21274-0701         | 1.763                       | 0.680                       | 1.396                       | 0.538                       | 2.006                       | 0.774                       | 1.172                       | 0.886                       | 1.167                       | 0.933                       |
| <b>HDS 3053</b>    | 0.153                       | 0.059                       | 0.258                       | 0.099                       | 0.195                       | 0.075                       | 0.037                       | 0.028                       | 0.010                       | 0.007                       |

BU1163



Figure 3. Apparent orbit of BU 1163. The green crosses represent the micrometric observations, the empty blue circles denote observations made with eyepiece interferometer, the red H the Hipparcos observations, the filled blue circles correspond to the speckle observations, and the magenta cross the last observation used in the calculation of the orbit, which provides the current relative position of the components in the apparent orbit.

Using these speckle measurements we have determined for the first time (Docobo et al. [2022](#page-13-0)), and simultaneously to A. Tokovinin (who sent a private communication to ORB6 then unknown to us), the visual orbit with very small rms, both in position angle and angular separation (1°.700 for  $\theta$  and 0.<sup>*n*</sup> 0028 for  $\rho$ ; see Table [3](#page-3-0)), and also with a good agreement with the common elements of the spectroscopic orbit (see Table [2](#page-3-0)). We have used the 3D methodology (Docobo et al. [2014](#page-13-0)) that we already commented in the Introduction with each of the five available observations, and they yield similar orbits with low residuals for the rest of the observations, proving that they are compatible.





Figure 4. Apparent orbit of CHR 240.

With these conditions, from the spectroscopic values of  $a_1$  sin *I* and  $a_2$  sin *I*, and the inclination and the semimajor axis of our orbit, it is possible to deduce the value of the orbital parallax

$$
\pi_{\text{Orb}} = \frac{a''}{a \text{ (in au)}} = 0''02676 \pm 0''00103. \tag{1}
$$

This value is slightly lower than the Gaia parallax  $(\pi_{Gaia} = 0''02831 \pm 0.00029)$ , and clearly smaller than that of Hipparcos  $(\pi_{\text{Hip}} = 0''03092 \pm 0''00095)$ , ANAPAR  $(\pi_{\text{Ana}} =$  $0''03055\pm 0.00136$ , and dynamical  $(\pi_{\text{Dyn}} = 0''03103\pm 0.00136)$ 0.00145), see Table [5](#page-5-0). This suggests a slight incompatibility between the visual and the spectroscopic orbits, and would merit a monitoring of this system.

<span id="page-7-0"></span>











With respect to the masses calculated for each parallax, they are all very similar (see Table [6](#page-6-0)), and they are well matched to the spectral types of the components, G3V-G9V, which have been obtained from the combined spectrum G6V and  $\Delta m = 0.72$ , which was deduced from the speckle registries.

There is also available an astro-spectroscopic solution by Gaia (Gaia Collaboration et al. [2016](#page-13-0), [2023](#page-13-0)), with a slightly larger period (0.581 yr). However their orbital elements do not



Figure 8. Apparent orbit of STF 2173.



Figure 9. Apparent orbit of HO 276.





agree with our solution, especially the angles I,  $\Omega$ , and  $\omega$  (see Table [2](#page-3-0)).

Recently a fourth companion has been detected in the system (R. A. Méndez 2023, private communication). First, it would be necessary to confirm that this new star is physically associated to the system. If so, depending on the separation to the couple AaAb, the perturbations produced by this new component might need to be considered in the dynamics of the close binary.

## 2.4. WDS 13317-0219 (HDS 1895, HIP 65982, HD 117635)

This star is an SB1, for which the orbit has a period of 1188 days (Latham et al. [2002](#page-13-0)). As a visual binary it was resolved by means of speckle interferometry from 2001, and several orbits exist as a result of those observations (Hartkopf et al. [2012](#page-13-0); Horch et al. [2012;](#page-13-0) Ren & Fu [2013;](#page-13-0) Tokovinin et al. [2020](#page-14-0); Videla et al. [2022](#page-14-0)). Some of these visual orbits take as fixed the common elements of the spectroscopic orbit.

Our spectral decomposition yields spectral types of  $G5.5V +$ K3V, therefore the expected masses are  $\approx 0.9 + 0.7 M_{\odot}$ . The parallax calculated using the ANAPAR methodology matches the one given by Gaia, and using the first, the obtained individual masses are  $0.886 + 0.716 \mathcal{M}_{\odot}$ . On the other hand, with our orbit and said parallaxes we got a total mass of  $M_1 + M_2 = 1.61 M_{\odot}$ , which is in good agreement with the previous result. Now, by using the mass function of the spectroscopic orbit  $f(M) = 0.00177297$ , and our orbital inclination 20°39:

$$
\frac{\mathcal{M}_2^3}{(\mathcal{M}_1 + \mathcal{M}_2)^2} = \frac{f(\mathcal{M})}{\sin^3 I} = 0.042.
$$
 (2)

However, with the values of the masses previously obtained we get:

$$
\frac{\mathcal{M}_2^3}{(\mathcal{M}_1 + \mathcal{M}_2)^2} = 0.143.
$$
 (3)

In order to match both values we need to lower the orbital inclination, but in this case the rms in  $\rho$  increases. It is also remarkable that the visual orbits with better rms, both in  $\theta$  and in  $\rho$ , have eccentricities lower than 0.55, whereas in the spectroscopic orbit it is 0.64.

# 2.5. WDS 15282-0921 (BAG 25 AaAb, HIP 75718, HD 137763)

The radial velocities of this SB2 began to be obtained in 1978, although the first SB1 spectroscopic orbit was calculated 13 yr later (Tokovinin [1991](#page-14-0)). One year later an SB2 orbit appeared (Duquennoy et al. [1992](#page-13-0)), which was recalculated much later (Halbwachs et al. [2018](#page-13-0)), although the period was very similar in the three orbits, close to 2.436 yr.

This binary was resolved in 2001 with the 6 m telescope at SAO (Balega et al. [2006b](#page-12-0)), and it was followed with speckle interferometry mainly by Horch et al. ([2012,](#page-13-0) [2015](#page-13-0), [2017](#page-13-0)) and Tokovinin et al. ([2015,](#page-13-0) [2016,](#page-13-0) [2020](#page-14-0)).

A first visual orbit calculated by Jancart et al. ([2005](#page-13-0)) shows positive residuals in  $\rho$  for the 23 available observations, which was later corrected (Tokovinin [2016b](#page-13-0)). Our solution, obtained by applying the 3D methodology (Docobo et al. [2014](#page-13-0)) improves the rms, and at the same time it breaks the systematic trend of the residuals in theta of the previous orbit. The application of said algorithm shows the coherence among most of the observations of this binary, and supplies a robust solution.

By using the Gaia parallax (see Table [5](#page-5-0)), our orbit yields a total mass  $\mathcal{M}_1 + \mathcal{M}_2 = 1.465 \pm 0.124 \mathcal{M}_{\odot}$ , and the mass ratio from the spectroscopic solutions are,  $\frac{\mathcal{M}_1}{\mathcal{M}_2}$  = 1.452  $\pm$  0.122 (using the Halbwachs et al. [2018](#page-13-0) orbit) and  $\frac{M_1}{M_2} = 1.494 \pm 0.031$  (using the Duquennoy et al. [1992](#page-13-0)) orbit). Therefore we can deduce the values of the individual

masses:

$$
\mathcal{M}_2 = 0.597 \pm 0.059\tag{5}
$$

in the first case, and:

$$
\mathcal{M}_1 = 0.878 \pm 0.075 \tag{6}
$$

$$
\mathcal{M}_2 = 0.587 \pm 0.050. \tag{7}
$$

We have decomposed the combined spectrum, G9V, in G8V +M0V. The masses obtained for the primary are a little below that corresponding to the spectral type G8V. In the case of the secondary component, it fits well the typical mass of a M0V spectral type.

#### 2.6. WDS 17304-0104 (STF 2173, HIP 85667, HD 158614)

Since this binary was discovered by W. Struve in 1830 (Aitken & Doolittle [1932](#page-12-0)), considering a period of around 46 yr, it has completed more than four revolutions, which together with its brightness, and its maximum angular separation of over one arcsecond, has made it a pair with a large number of visual observations in the last 200 yr, including more than 40 of speckle monitoring.

That is why numerous orbits have been calculated, both as a visual (Flammarion [1878;](#page-13-0) Lewitzky [1896;](#page-13-0) See [1896](#page-13-0); Lewis [1906;](#page-13-0) Doberck [1910;](#page-13-0) Aitken [1914;](#page-12-0) Lohse, included in Aitken & Doolittle [1932](#page-12-0); Duncombe & Ashbrook [1952](#page-13-0); Starikova [1976;](#page-13-0) Wilson [1976](#page-14-0); Heintz [1994;](#page-13-0) Söderhjelm [1999](#page-13-0); Pourbaix [2000](#page-13-0)), and as spectroscopic SB2 (Batten et al. [1971,](#page-12-0) [1991](#page-12-0); Duquennoy & Mayor [1991](#page-13-0); Pourbaix [2000](#page-13-0)). In fact, Pourbaix solution takes into account simultaneously both  $(\theta, \rho)$ , and the radial velocities for its determination. The orbit proposed in this paper shows the best rms of all, both in  $\theta$  and in  $\rho$ .

This binary is included in the emblematic catalogs of measurements of Burham ([1906](#page-12-0)), with the number 8083, and Aitken & Doolittle ([1932](#page-12-0)), with the number 10598. In the last one, Aitken says that "The parallax is well determined. The trigonometric value is  $+0''052$  (Yale), the spectroscopic.  $0''063$ (Mt W) or  $0''062$  (DAO), the dynamic,  $0''066$  (J & F) or  $0''063$  $(R & M)$ ."

The spectral type of this binary was listed mainly as a G8IV-V, however it appears as G5V (Sharma et al. [2020](#page-13-0)) or G6V (Houk & Swift [1999](#page-13-0)) in the last publications. In the first of these two cases, the decomposition yields G4.5V+G5V, whereas in the second it gives G6V+G6V, as the magnitude difference between the components is only 0.04 (6.06–6.10). In this way, the expected total mass is 1.96 or 1.94  $\mathcal{M}_{\odot}$ , respectively.

Gaia lists the parallaxes of both components: 0″05850 and 0″06071, of which the mean value is 0"05960. Considering our orbital solution, the spectral types G4.5V+G5V, and using the Hipparcos and Gaia parallaxes, as well as the dynamical and ANAPAR parallaxes, we get the results shown in Table [6](#page-6-0).

As for the spectroscopic orbits, and taking into account the inclination of 99◦ from our orbit, the solution of Batten et al. ([1991](#page-12-0)) assigns the largest mass to the secondary component  $(0.905 + 1.033 \, \mathcal{M}_{\odot})$ , whereas the orbit by Batten et al. ([1971](#page-12-0)) yields a total mass of 2.145  $M_{\odot}$ . The other two orbits (Duquennoy & Mayor [1991](#page-13-0); Pourbaix [2000](#page-13-0)) lead to total masses slightly lower than 2  $\mathcal{M}_{\odot}$ .

With respect to the orbital parallaxes, and making use of the value of *a* sin *I* from each of the spectroscopic orbits, and the

- 1. 0″06071 (with the Pourbaix orbit).
- 2. 0″06002 (Batten et al. orbit).
- 3. 0″05987 (Duquennoy & Mayor orbit).
- 4. 0″05803 (Batten, Fletcher & West orbit).

As we can see, all the parallaxes for this binary are in good agreement.

This binary shows a large proper motion. According to the data from Hipparcos (Perryman et al. [1997;](#page-13-0) van Leeuwen [2007](#page-14-0)): (−127.77, −168.61) mas yr−<sup>1</sup> . Gaia, for its part (Gaia Collaboration et al. [2016,](#page-13-0) [2018](#page-13-0)), gives separate values for each component: (−138.31155679907, −144.41982410308927) mas  $yr^{-1}$ , and (-120.59892576351368, -208.53898150434344) mas  $yr^{-1}$ , which are affected by the orbital motion.

#### 2.7. WDS 19598-0957 (HO 276, HIP 98416, HD 189340)

Burnham ([1906](#page-12-0)) points in his catalog of measurements that in 1887 G. W. Hough described this star as elongated, but he was not able to resolve it, as it was not possible either in 1890 by the same S. W. Burnham, between 1903 and 1906 by E. Doolittle, and in 1906 by R. G. Aitken (Burnham [1906](#page-12-0)). It was Finsen ([1962](#page-13-0)) the first to obtain the position angle and the separation of this short-period binary (less than 5 yr). Burnham also alerted of its notable proper motion. The Gaia DR2 (Gaia Collaboration et al. [2016](#page-13-0), [2018](#page-13-0)) following values for the proper motion are listed as:  $-272.764$  and  $-404.804$ .

The first orbit was announced by Baize ([1990](#page-12-0), [1992](#page-12-0)), as circular and with a period of 9.7 yr. However, Duquennoy & Mayor ([1991](#page-13-0)) obtained almost simultaneously SB1 and SB2 solutions with periods 4.649 and 4.901 yr, respectively, showing that the orbital period really was half of that determined by Baize ([1990,](#page-12-0) [1992](#page-12-0)) and that the orbital eccentricity was close to 0.6. Despite this fact, in the following years long-period low-eccentricity orbits were determined (Hartkopf et al. [1996](#page-13-0); Söderhjelm [1999](#page-13-0)).

Pourbaix ([2000](#page-13-0)) calculated a solution fitting both the visual measurements and the radial velocities. Such an orbit showed almost from the publication years systematically positive residuals in the position angle, probably because the radial velocities do not cover strategical parts of the orbit, and that is why it was revised by Tokovinin ([2017](#page-13-0)). The orbit presented in this paper clearly improves the rms of all the previous orbits.

The mean of the magnitude differences between the components from the speckle measurements is 1.59, which is coherent with the visual magnitudes from Hipparcos, 6.22 and 7.83, given in the WDS catalog. With respect to the combined spectrum, according to the different measurements gathered in Simbad (Roman [1955;](#page-13-0) Eggen [1962;](#page-13-0) Malaroda [1975;](#page-13-0) Cannon & Pickering [1993;](#page-12-0) Houk & Swift [1999;](#page-13-0) Gray et al. [2003](#page-13-0)), it is between F8 and G2. For example, with F9V (Gray et al. [2003](#page-13-0)) and the speckle magnitude difference, F6V and G8V are deduced, whereas with G2V (Houk & Swift [1999](#page-13-0)) the decomposition yields F9.5V and K1V. In the first case the standard masses would be  $1.25 + 0.94 = 2.19 \mathcal{M}_{\odot}$ , and in the second  $1.08 + 0.86 = 1.94 M_{\odot}$ .

Table [6](#page-6-0) shows the values of the masses obtained from the different parallaxes.

As for the orbital parallax, and also the masses derived, should be the most precise, but for it to be true both orbits (visual and spectroscopic) have to be of the best quality, which is not this case. The spectroscopic orbit must be improved by filling the whole orbital phase with radial velocities because currently there are strategic areas that are not well covered, mainly close to the maximal and the minimal value of the radial velocity.

# 2.8. WDS 21274-0701 (HDS 3053, HIP 105947, HD 204236)

This is a hierarchical triple system composed by a binary, for which the main component is in turn an SB1 (Tokovinin [2018b](#page-13-0)). The initial binary, components A and B, was discovered by Hipparcos (Perryman et al. [1997](#page-13-0)), whereas Nordström et al. ([2004](#page-13-0)), by studying the radial velocities of the system, detected the spectroscopic subcomponent, AaAb, for which the orbital period is 8.7279 days (see Table [4](#page-4-0)).

Several orbits have been calculated (Balega et al. [2006a](#page-12-0); Mason et al. [2010](#page-13-0); Tokovinin et al. [2015](#page-13-0); Tokovinin [2018b](#page-13-0); Mitrofanova et al. [2021](#page-13-0)) from the speckle observations, which were performed mainly by Balega et al. ([2002,](#page-12-0) [2006,](#page-12-0) [2007](#page-12-0), [2013](#page-12-0)), Tokovinin et al. ([2010a](#page-13-0), [2010b](#page-13-0), [2014,](#page-13-0) [2015,](#page-13-0) [2016](#page-13-0)), and Mitrofanova et al. ([2021](#page-13-0)), and occasionally by Mason et al. ([1999](#page-13-0), [2010](#page-13-0)) and Horch et al. ([2008,](#page-13-0) [2009](#page-13-0), [2011](#page-13-0)). Also, Tokovinin ([2018b](#page-13-0)) completed his visual solution with SB2 elements by using three radial velocity measurements, and at the same time, he determined the position of the ascending node. Moreover, the orbit as an SB1 of Ab around Aa was published in the same article.

From visual magnitudes 7.97 and 9.14 for the A and B components, and a combined spectral type of G0V, its decomposition yields F8.5V and G8V for AaAb and B, respectively. If we now separate the spectral type F8.5V of AaAb as a function of the magnitude difference,  $\Delta m$ , we get the results shown in Table [7,](#page-10-0) in which we have assumed a mass of 0.94 for component B (spectral type G8V).

On the other hand, by using the values of  $a''$  and the inclination of the orbit of B with respect to AaAb, along with *a* sin *I* from the SB2 orbit, it is deduced an orbital parallax of:

$$
\pi_{\text{Orb}} = \frac{a''}{a \text{ (in au)}} = 0''01617,\tag{8}
$$

which, when inserted in the expression,

$$
\mathcal{M}_{Aa} + \mathcal{M}_{Ab} + \mathcal{M}_B = \frac{\left(\frac{a''}{\pi_{\text{Otb}}}\right)^3}{P^2},\tag{9}
$$

yields the value of the total mass of the triple system, 2.443  $M_{\odot}$ , which is close to the value of  $\Delta m = 7$  $\Delta m = 7$  of Table 7. With these individual masses, the mass function,  $f(M) =$ 0.0184921, of this orbit yields an inclination of  $I_{12} = 70^{\circ}$ . Here we have used the subscript 12 to denote orbit of Ab with respect to Aa. However, if we consider the Gaia DR3 parallax,  $0''01549$ , slightly lower than the orbital parallax, Equation  $(9)$ gives a total mass of 2.80  $M_{\odot}$ , which is close to the case of  $\Delta m = 4.5$ , with masses  $\mathcal{M}_{Aa} = 1.23$  (Sp. F6.5V), and  $M_{Ab} = 0.63$ , and an orbital inclination  $I_{12} = 39^{\circ}5$ .

Table 7 Spectral Decomposition of HDS 3053 According To The Magnitude Difference of AaAb

<span id="page-10-0"></span>

| $\Delta m$ | Spectral type<br>Aa | Spectral type<br>Ab | Mass Aa<br>$(\mathcal{M}_{\odot})$ | Mass Ab<br>$(\mathcal{M}_{\odot})$ | Mass B<br>$(\mathcal{M}_{\odot})$ | Total mass<br>$(\mathcal{M}_{\odot})$ |
|------------|---------------------|---------------------|------------------------------------|------------------------------------|-----------------------------------|---------------------------------------|
|            | F <sub>6</sub> V    | G1.5V               | 1.25                               | 1.05                               | 0.94                              | 3.20                                  |
|            | <b>F5.5V</b>        | G9V                 | 1.29                               | 0.90                               | 0.94                              | 3.13                                  |
|            | <b>F5.5V</b>        | K3V                 | 1.29                               | 0.78                               | 0.94                              | 3.01                                  |
| 4          | F <sub>6</sub> V    | K <sub>6</sub> V    | 1.25                               | 0.69                               | 0.94                              | 2.88                                  |
| 5          | F7V                 | M <sub>0</sub> V    | 1.21                               | 0.57                               | 0.94                              | 2.72                                  |
| 6          | F8V                 | M2V                 | 1.18                               | 0.44                               | 0.94                              | 2.56                                  |
|            | <b>F8.5V</b>        | M3V                 | 1.15                               | 0.37                               | 0.94                              | 2.46                                  |

Note. Column 1 contains the magnitude difference, with a step of 1 magnitude; columns 2 and 3 show the spectral types of the components Aa and Ab, respectively, calculated from  $\Delta m$ ; columns 4 and 5 the corresponding calibrated masses; column 6 yields the mass of the component B; and column 7 the total mass. All masses are given in units of solar mass.



| Star            | $M_{\rm VA}$ | $M_{\rm VR}$ | $L_A(L_{\odot})$ | $L_B(L_{\odot})$ |
|-----------------|--------------|--------------|------------------|------------------|
| <b>BU1163</b>   | 3.32         | 3.71         | $3.79 + 0.21$    | $2.67 + 0.15$    |
| <b>CHR 240</b>  | 4.14         | 4.82         | $1.82 + 0.04$    | $1.01 + 0.02$    |
| $S$ 634 AaAb    | 4.91         | 5.63         | $0.93 + 0.19$    | $0.51 + 0.11$    |
| <b>HDS 1895</b> | 5.49         | 6.81         | $0.58 + 0.05$    | $0.23 + 0.02$    |
| BAG 25 AaAb     | 5.45         | 8.94         | $0.60 + 0.08$    | $0.06 + 0.01$    |
| STF 2173        | 4.91         | 4.95         | $0.94 \pm 0.11$  | $0.91 \pm 0.11$  |
| HO 276          | 4.32         | 5.93         | $1.56 + 0.02$    | $0.41 + 0.01$    |
| <b>HDS 3053</b> | 4.03         | 5.20         | $1.99 + 0.17$    | $0.73 + 0.06$    |

Table 9 Temperature and Metallicity



## 3. Luminosities and Ages

In order to calculate the luminosities with the expression (Torres [2010](#page-14-0)):

$$
\log \frac{L}{L_{\odot}} = -0.4(M_V - V_{\odot} - 31.572 + (BC_V - BC_{\odot})).
$$
 (10)

The value of  $V_{\odot}$  was adopted from Torres ([2010](#page-14-0)) and the bolometric corrections adopted from Pecaut & Mamajek ([2013](#page-13-0))

As usual,  $L_{\odot}$  and  $V_{\odot}$  are the luminosity and the apparent visual magnitude of the Sun,  $BC_V$  and  $BC_{\odot}$  are, respectively,



Figure 11. HR diagram and isochrones for BU 1163.



Figure 12. HR diagram and isochrones for CHR 240.

the bolometric corrections of the star and the Sun in the V band, and  $M_V$  is the absolute V magnitude of the star.

To obtain the  $M_V$  of the components, the apparent V magnitudes were corrected by the interstellar extinction,  $A_V$ , using the Parenago formula, depending on the distance,  $d$ , and the galactic latitude, b, as described in Malkov et al. ([2018](#page-13-0)):

$$
A_V = \frac{a_0 \beta}{\sin |b|} (1 - e^{\frac{-d \sin |b|}{\beta}})
$$
 (11)

<span id="page-11-0"></span>

Figure 13. HR diagram and isochrones for S 634 AaAb.



Figure 14. HR diagram and isochrones for HDS 1895.



Figure 15. HR diagram and isochrones for BAG 25 AaAb.

where  $a_0$  is the absorption per kpc and  $\beta$  is the vertical scale of the absorbing matter distribution, with an estimated value of 1.6 mag kpc−<sup>1</sup> and 114 pc, respectively (Sharov [1964](#page-13-0)). After the extinction was applied, the ANAPAR parallaxes, shown in the Table [8](#page-10-0), were used.

Table [8](#page-10-0) shows the name of the star in the first column, the calculated  $M_V$  of the components appear in the second and third



Figure 16. HR diagram and isochrones for STF 2173.



Figure 17. HR diagram and isochrones for HO 276.



Figure 18. HR diagram and isochrones for HDS 3053.

columns, and the luminosities are shown in the fourth and fifth columns.

To obtain information associated with system ages, we used their metallicity values from Holmberg et al. ([2009](#page-13-0)), Gáspár et al. ([2016](#page-13-0)), and Soubiran et al. ([2016](#page-13-0)). We applied the relations between the spectral type and effective temperature given by de Jager & Nieuwenhuijzen ([1987](#page-13-0)). The isochrones were provided by MIST version 1.2 (Paxton et al. [2011](#page-13-0),

<span id="page-12-0"></span>[2013,](#page-13-0) [2015;](#page-13-0) Choi et al. 2016; Dotter [2016;](#page-13-0) Paxton et al. [2018](#page-13-0)). According to their masses, we set initial  $v/v_{\text{crit}} = 0.0$  for all the systems. The values utilized to calculate the isochrones can be seen in Table [9.](#page-10-0)

We plotted the pair  $(T \in \text{eff}, \log \frac{L}{L_{\odot}})$  of the primary and secondary components of the systems in HR diagrams (see Figures [11](#page-10-0)–[18](#page-11-0)) showing the isochrones of the most probable ages of the system. The data do not support a definitive value for some system ages. However, we can see that the calculated luminosities are consistent with system coevolution indicating that both components have the same origin.

## 4. Conclusions

Once again, the HRCam attached to the 4.1 m SOAR telescope confirms the suitability of this instrumentation  $+$ telescope to continue performing speckle observations in the future, especially of austral close binaries.

In the present research, using this class of measurements obtained since 2019–2022, the authors have been able to improve the visual orbits of eight binaries taking into account that each of these binaries has also an spectroscopic orbit. So, in these conditions the information achieved is maximum both regarding the different parallaxes: orbital, dynamical, ANA-PAR, and those corresponding to the Hipparcos and Gaia missions, and on the other hand concerning the values of the masses derived from the parallaxes. In all of the cases, individual masses have been reported.

It is important to recommend also the improving of some of the spectroscopic orbits involved in the present work. RV velocities close to strategic points of the orbits are necessary in order to determine orbital parallaxes with high quality.

In addition to this, using absolute luminosities with data regarding the metallicities and effective temperatures, the position of the sixteen components in the HR diagram against the most suitable isochrones produced by MIST has been plotted. All of these plots show similar ages for the components and are coherent with a coevolution and common origin context.

This is the fourth paper on binaries produced by the collaboration between the University of Chile and the University of Santiago de Compostela (Galicia, Spain).

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Le Contel et al. [2001](#page-13-0)) compiled principally by Dr. Paul Couteau; the historical database of micrometric measurements provided by the WDS (Mason et al. [2001b](#page-13-0)) the Catalogue of Interferometric Measurements of Binary Stars (WDS INT4; Hartkopf et al. [2001b](#page-13-0)); and the Sixth Catalogue of Orbits of Visual Binary Stars (WDS ORB6; Hartkopf et al. [2001a](#page-13-0)), all of them maintained at USNO.

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Facility: SOAR.

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