

Journal of Engineering Research and Reports

21(7): 59-70, 2021; Article no.JERR.78407 ISSN: 2582-2926

## Surface Roughness Characterization for Stress Concentration Factor Predictions: A Bayesian Learning Approach

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## Author's contribution

The sole author designed, analyzed, interpreted and prepared the manuscript.

## Article Information

DOI: 10.9734/JERR/2021/v21i717479 <u>Editor(s)</u>: (1) Dr. Djordje Cica, University of Banja Luka, Bosnia and Herzegovina. <u>Reviewers:</u> (1) Ogundokun Roseline Oluwaseun, Landmark University, Nigeria. (2) Cosmas Ifeanyi Nwakanma, Federal University of Technology, Nigeria. Complete Peer review History, details of the editor(s), Reviewers and additional Reviewers are available here: <u>https://www.sdiarticle5.com/review-history/78407</u>

Original Research Article

Received 03 October 2021 Accepted 08 December 2021 Published 13 December 2021

## ABSTRACT

The surface roughness has an important influence on the fatigue life of the structures. The fatigue life reduces due to the stress concentration caused by surface roughness. The stress concentration governs the fatigue crack initiation and propagation. The accurate acquisition of the stress concentration factor of rough surfaces is a key issue in determining fatigue life. Nevertheless, semi-empirical models may be biased for various machining processes. Besides, finite element method simulations cannot give explicit expression of the stress concentration factor. Bayesian learning can construct accurate prediction models which offering a number of additional advantages. In this paper, based on several data pairs constructed by finite element method, the correlation expression between the stress concentration factor and statistical roughness parameters of surfaces is established quickly through Bayesian learning. Compared with some other semi-empirical models, the accuracy and stability of the proposed method are certified. This paper provides a simple and efficient approach to determine the stress concentration factor for rough surfaces under different processing conditions.

Keywords: Surface roughness; stress concentration factor; statistical roughness parameters; Bayesian learning.

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### 1. INTRODUCTION

The fatigue life of structures is known to influence the service life of the structures highly. Moreover, the fatigue life depends on the surface quality, which will lead to the fatigue crack. There are three parameters to describe surface quality: (i) surface roughness, (ii) residual stress, (iii) microstructure. For some materials, especially aluminium alloy, surface roughness is the dominant parameter for fatigue life. Surface roughness introduces local stress concentration governing the crack initiation and propagation. The experiments show that the fatigue strength increases with a decrease in the surface roughness [1]. Therefore, the effect of surface roughness on the fatigue life cannot be neglected. Surface roughness is described roughness parameters. through statistical Traditional fatigue life predictions use empirical reduction factors to calculate the effect of surface roughness [2-5]. However, it is not a simple way due to many materials and machining processes. The empirical reduction factors need to be found for the same machining process through timeconsuming testing. Beyond that method, the effect of statistical roughness parameters on the fatigue life is proposed in several approaches. In those methods, surface roughness is considered as causing stress concentration to reduce the crack initiation and propagation life. The effect can be described through the fatigue stress concentration factor  $K_{f}$ . It is defined as

$$K_f = \frac{\sigma_D^{(\text{smooth})}}{\sigma_D^{(\text{rough})}} \tag{1}$$

And it can be expressed by the stress concentration factor  $K_t$  according to

$$K_{f} = 1 + q(K_{t} - 1) \tag{2}$$

This consideration requires the calculation of the stress concentration factor to evaluate the fatigue life of engineering components [6].

There are two methods to study the influence of surface roughness on the stress concentration factor. One method is a semi-empirical formula, and the other is a numerical simulation. Some researchers have treated surface roughness as a series of microscopic notches. A stress concentration factor  $K_t$  is introduced. Neuber [7] considered that the surface topography is characterized by adjacent continuous gaps and proposed to estimate  $K_t$  according to

$$K_t = 1 + n\sqrt{\lambda R_z \rho^{-1}}$$
(3)

where  $\lambda$  refers to the ratio between spacing and height of surface irregularities, and *n* represents the conditions (where *n*=1 represents the shear and *n*=2 represents tensile). Nevertheless, the actual value of  $\lambda$  is hard to define for generic surface textures. Arola and Ramulu [8] suggested a different formula, where

$$K_t = 1 + n \left( R_a / \rho \right) \left( R_y / R_z \right)$$
(4)

The surface topography is simplified as an ideal sinusoidal micro-notch, and for AISI 430 CR steel, this expression can estimate the fatigue stress concentration factor ( $K_i$ ) more accurately. Also, Andrews and Sehitoglu [9] treated the surface topography as a more common semi-elliptical notch and gave the expression as

$$K_t = 1 - 0.719 \exp\left[-0.476 \left(\frac{b}{a}\right)\right] \times \left[1 + 2\left(\frac{c}{\rho}\right)^{1/2}\right]$$
(5)

where the notch width and notch spacing are denoted as a and b, the notch depth and tip radius are symbolized by c and  $\rho$ . The above methods simplify the surface topography to microscopic notches, making it difficult to estimate the surfaces under different processing conditions accurately. Another method to study the problem calculates  $K_t$  from finite element method (FEM) simulations of the measured surface topography. As et al. [10,11] used the FEM description of the surface profile to calculate  $K_t$ , the surface topography was measured using a white light interferometry microscope. Suraratchai et al. [12] fitted the measured machined surface topography and analyzed  $K_t$  by FEM simulations. However, the FEM simulations cannot give the explicit expression of the stress concentration factor. Bayesian learning method performs well in constructing prediction models. Tripping et al. [13,14] introduced the bayes theory and its combination with relevance vector machine systematically. Whereafter, Sivia at al. [15]and Gelman et al. [16] had respectively written a comprehensive exposition of the derivation of Bayesian learning. Sergio [17] stated Bayesian learning from a Bayesian and optimization perspective in machine learning. Shufei Ge et al. [18] derived a Markov chain Monte Carlo (MCMC) algorithm to the Bayesian learning. About Markov chain Monte Carlo (MCMC) algorithm, Andrieu et al. and Walter et al. [19.20] had detailed introductions in the articles. And Bhattacharya et al. [21] completed Gibbs inference in Bayesian posterior learning. Meanwhile, Hagiwara et al. [22,23] further developed hierarchical Bayesian model on multimodal information. At present, Bayesian learning has been widely used in a number of fields. Yuen et al. [24] summarized developments of Bayesian model in civil engineering. Ching et al. [25] and Kamariotis et al. [26] modeled in detail the structural health monitoring with Bayesian learning using Gibbs sampler. Huang et al. [27], Zhang et al. [28] and Li et al. [29] detected structural damage based on hierarchical sparse Bayesian learning. Chatterjee et al. [30] determined unknown coefficients by Bayesian learning in optimization framework based robust design. Fox et al. [31] imposed a two-level regression model based Bayesian estimation in an item response theory model. Xiaochen Ma et al. [32] combined sparse Bavesian learning with least squares estimation for materials' measurement of echo reduction.

This paper establishes the correlation expression between the stress concentration factor and statistical roughness parameters of surfaces through Bayesian learning. The datasets of  $K_t$ are first constructed by FEM simulations of surface topography. Subsequently, Bayesian learning with Gibbs sampler is employed to predict expression between stress concentration factor and statistical roughness parameters. The predicted values are in good agreement with the FEM simulations compared with some other semi-empirical models, which certified the accuracy and stability of the proposed method.

## 2. MATERIALS AND METHODS

#### **2.1 Finite Element Method**

#### 2.1.1 Rough surfaces

The rough surfaces are generated randomly through an open-source code in MATLAB [33]. The usability of this code has been experimentally verified by the proposer. According to the study [5], machined surface roughness ( $R_a$ ) values over 0.1 µm, which strongly influences fatigue life. With the surface roughness ( $R_a$ ) being less than 0.1 µm, this effect diminishes as cracks initiate due to persistent slip bands or grain boundaries. Therefore, when the surface topography is generated, the value of  $R_a$  is set to be greater than 0.1 µm. Moreover, the lower frequency

cutoff and the upper frequency cutoff are incorporated through a slight modification. The surfaces can also be assigned from actual rough topographies through a white light interferometry microscope. The profile of the generated rough surface is shown in Fig. 1, where *x* represents the horizontal position of the rough central axis, and *L* represents the width of the rough surface. x/L represents the dimensionless relative position.



Fig. 1. The profile of generated surface topography

Surface roughness is characterized through statistical roughness parameters such as  $R_a$  (average roughness),  $R_y$  (peak-to-valley height roughness),  $R_z$  (10-point roughness), and  $\rho$  (the average profile valley radius). These parameters are defined in terms of the profile height distribution (*z*) recorded, in respect to the mean line, over an assessment length (*L*) according to

$$R_a = \frac{1}{L} \int_0^L |z(x)| dx \tag{6}$$

$$\boldsymbol{R}_{y} = \left| \boldsymbol{z}_{max} - \boldsymbol{z}_{min} \right| \tag{7}$$

$$R_{z} = \frac{1}{5} \left[ \sum_{i=1}^{5} (z_{i})_{max} + \sum_{j=1}^{5} |(z_{j})_{min}| \right]$$
(8)

where  $(z_i)_{max}$  and  $(z_j)_{min}$  are the five higher local maxima and lower local minima, respectively, of the profile height distribution (z).

#### 2.1.2 Finite element method simulations

In FEM simulations, the assumption of isotropic and homogeneous materials is introduced. When calculating the stress concentration factor, only

the linear elastic behavior of the material should be considered. Firstly, a smooth finite element model is established by using the commercial software ABAQUS. Then, to realize the surface of model is the above profile generated by MATLAB, MATLAB programming is used to change the surface node coordinates of the generated model.

Fig. 2 shows the example of the final generated finite element model and simulation performed to determine  $K_{t}$ .



# Fig. 2. Finite element model of determining the stress concentration factor

For the turning process, the specimens are rotated in a lathe. This process produces circumferential grooves through a repeated way, which can be modelled by an axisymmetric model. The height of the model is 5000 µm, and the nominal length of the rough surface is 20000 µm. Uniform tensile load is applied to both ends of the boundary. Young's module E is 72 GPa, and Poisson's ratio v is 0.33. In FEM simulations, axisymmetric quadrilateral elements (CAX4) are adopted to discretize the model, in which the meshes are gradually coarsened along the r-axis from top to bottom. For one of rough surfaces R<sub>y</sub>=1.191023,  $(R_a=0.192818,$ R<sub>z</sub>=1.179942,  $\rho$ =569.1562), the minimum mesh size of the adjacent surface topography is 0.4 µm. As preparation, the accuracy of our computational results has been guaranteed by convergence tests.

The stress concentration factor of each point on the surface topography is defined as

$$K = \frac{\sigma}{\sigma_{nom}} \tag{9}$$

where  $\sigma$  is the Von Mises equivalent stress, and  $\sigma_{nom}$  is the nominal Von Mises equivalent stress of the cross-section, as shown in Fig. 3, where *x* represents the horizontal position of the rough central axis, and *L* represents the width of the rough surface. *x*/*L* represents the dimensionless relative position.



# Fig. 3. The stress concentration factor *K* of each point on the surface topography

And the maximal Von Mises equivalent stress obtained by the calculation is then divided by the nominal Von Mises equivalent stress due to the applied load to determine the stress concentration factor  $K_t$  classically, expressed as

$$K_t = \frac{\sigma_{max}}{\sigma_{nom}} \tag{10}$$

where  $\sigma_{max}$  is the maximal Von Mises equivalent stress along with the surface topography.

#### 2.1.3 Data

By FEM simulations, the statistical roughness corresponding parameters, and stress concentration factor of 41 different specimens have obtained, which constitutes the datasets, as shown in Table 1. The datasets consist of 41 data pairs, including  $R_a$ ,  $R_y$ ,  $R_z$ ,  $\rho$  these four independent variables that characterize the properties of rough surface and  $K_t$  which describe the stress concentration caused by surface roughness. The value of  $R_a$  is set to be greater than 0.1 µm and less than 6.4 µm. The range of  $R_v$ ,  $R_z$ ,  $\rho$  and  $K_t$  are (1.19, 44.81), (1.17, 44.53), (16.14, 569.16) and (1.04, 2.73) to verity that this method is applicable to rough surfaces under various processing conditions.

Number	<i>R<sub>a</sub></i> /µm	<i>R</i> ,∕µm	<i>R₂</i> /µm	ρ/µm	K <sub>t</sub>
1	3.555986	26.30374	26.11672	16.99651	2.153361439
2	4.2303	22.98283	22.69772	25.07418	2.105857375
3	5.440313	31.41201	31.00602	17.03947	2.638873261
4	0.772174	4.512271	4.475618	137.147	1.153786981
5	4.025152	25.22172	25.04139	23.22475	1.963668871
6	5.583996	30.33734	29.96099	19.03229	2.519425105
7	4.726791	30.61076	30.35646	26.28119	1.983688209
8	0.331772	2.402115	2.379683	246.3604	1.09061872
9	2.4	12.32988	12.24221	36.10878	1.509358561
10	3.693573	26.18617	25.79348	25.35032	2.040652054
11	0.192818	1.191023	1.179942	569.1562	1.03880591
12	6.000485	36.44235	36.27377	17.45057	2.673570711
13	3.252341	23.35157	23.11154	31.73201	1.863292314
14	1.92	9.863903	9.793769	45.11696	1.402105278
15	2.404957	14.19217	13.96398	39.43441	1.640159853
16	2.400194	14.57694	14.50951	38.80922	1.622350349
17	1.721862	11.27853	11.23405	56.88085	1.37554257
18	5.550449	33.70917	33.55324	18.84812	2.535736852
19	7.066363	44.00704	43.72766	16.13747	2.733849542
20	1.018625	6.101202	6.014407	93.90284	1.24962646
21	2.226748	11.31604	11.21579	41.2961	1.480055216
22	0.792587	3.752242	3.695435	101.3596	1.185491742
23	5.69759	40.40472	39.95214	17.55418	2.184433519
24	1.121263	7.949373	7.830165	83.26314	1.299609142
25	4.074499	24.40481	24.05763	41.9364	2.12358941
26	5.337771	34.96346	34.82555	18.41903	2.325390202
27	1.118098	7.006034	6.955942	83.35896	1.247479891
28	5.59575	32.3095	31.89191	16.57165	2.690652606
29	2.346066	16.63724	16.45088	42.45231	1.459829098
30	6.398332	44.80768	44.53094	16.74337	2.546558207
31	3.053939	17.03504	16.92747	39.79985	1.681130644
32	1.894048	12.40639	12.35745	51.71469	1.416110263
33	5.045286	36.30095	36.14158	18.61619	2.129087822
34	3.890513	23.19896	22.96311	33.14648	1.892614248
35	4.597006	21.76301	21.43352	17.53594	2.207043075
36	3.431884	20.05454	19.89164	30.91224	1.751842258
37	3.400587	23.04051	22.9307	28.43874	1.743377001
38	4.118261	24.06545	23.86996	25.78116	1.918798908
39	1.505916	7.129261	7.021326	53.36182	1.362512558
40	0.606735	37.02597	36.87318	27.83285	2.536359788
41	0.517418	3.715022	3.676836	199.0674	1.125912072

Table 1. Databa	se constructed	by FEM	simulations
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Table 2. Some empirical models for estimating the stress concentration factor  $K_t$ 

Empirical models	Literature
$K_t = 1 + 2\sqrt{\lambda R_z \rho^{-1}}$	Neuber
$K_t = 1 + 2R_a R_y \left(R_z \rho\right)^{-1}$	Arola-Ramulu

### 2.2 Bayesian Learning

According to the existing models, several models propose the expression between  $K_t$  and the statistical roughness parameters of surfaces, as shown in Table 1.

Those models can be rewritten as linear models. Therefore, the expression is assumed as

$$\ln(K_t - 1) = \omega_1 \ln(R_a/\rho) + \omega_2 \ln(R_a/R_y) + \omega_3 \ln(R_a/R_z) + \omega_4$$
(11)

The Bayesian learning [14-17] with Gibbs sampler [18-22] is used to estimate  $\boldsymbol{\omega}$ .

#### 2.2.1 Bayesian theorem

According to the Bayesian theorem and the proposed methods of early scholars, the expression can be written as a linear combination of function  $\Phi$  of the form

$$y_i(\mathbf{X}_i, \boldsymbol{\omega}) = \sum_{m=0}^{M} \omega_m f_m(\mathbf{X}_i) = \boldsymbol{\omega}^T \boldsymbol{\Phi}$$
(12)

where  $y_i$  (**X**<sub>*i*</sub>, **\omega**) represents the function of predicted  $K_t$ , expressed as

$$y_i(\mathbf{X}_i, \mathbf{\omega}) = \ln\left[\left(K_i\right)_i - 1\right]$$
(13)

 $\mathbf{X}_i$  represents the independent variables, and the  $\mathbf{\Phi}$  is a function of  $\mathbf{X}_i$ . The  $\omega_m$  are the parameters of the model and are generally called weights.

To support additive noise between  $y_i(\mathbf{X}_i, \boldsymbol{\omega})$  and  $\boldsymbol{\omega}^T \boldsymbol{\Phi}$ , the Eq. (7) will be rewritten as

$$y_i(\mathbf{X}_i, \boldsymbol{\omega}) = \sum_{m=0}^{M} \omega_m \phi_m(\mathbf{X}_i) + \varepsilon$$
(14)

where  $\varepsilon$  is assumed to be Gaussian distribution expressed as

$$P(\varepsilon|\tau) = N(\varepsilon|0,\tau^{-1})$$
(15)

and *t* follows Gamma distribution as

$$P(\tau) = \Gamma(\tau|a,b) = b^a \tau^{a-1} e^{-b\tau} / \Gamma(a)$$
(16)

Also, to complete the specification of hierarchical prior, choose a zero-mean Gaussian prior distribution over  $\boldsymbol{\omega}$ .

$$P(\boldsymbol{\omega}|\boldsymbol{\alpha}) = N(\boldsymbol{\omega}|0, \boldsymbol{\alpha}^{-1})$$
(17)

Suitable priors thereover are Gamma distribution, which is expressed as

$$P(\boldsymbol{a}) = \Gamma(\boldsymbol{a}|c,d) = \prod_{j=1}^{n} d^{c} \alpha_{j}^{c-1} e^{-d\alpha_{j}} / \Gamma(c)$$
(18)

In Bayesian theorem, the basic idea is to convert a prior probability density function for the parameters  $\boldsymbol{\omega}$  into a posterior distribution with the data  $\boldsymbol{D}$  in the form

$$P(\boldsymbol{\omega}|\mathbf{D}) = \frac{P(\mathbf{D}|\boldsymbol{\omega})P(\boldsymbol{\omega})}{P(\mathbf{D})}$$
(19)

Thus, the posterior PDF is derived as below by Bayesian theorem,

$$P(\boldsymbol{\omega}, \tau, \boldsymbol{\alpha} | \mathbf{D}) = [P(\mathbf{D} | \boldsymbol{\omega}, \tau) P(\boldsymbol{\omega} | \boldsymbol{\alpha}) P(\tau)$$

$$P(\boldsymbol{\alpha})] / P(\mathbf{D})$$
(20)

#### 2.2.2 Gibbs sampler

The process for Gibbs sampler is as below [15],

(i) select the training data pairs,

(ii) initialize the parameters  $\alpha(0)$  and  $\tau(0)$ ,

sample the parameter  $\boldsymbol{\omega}(n) \sim P(\boldsymbol{\omega}|\boldsymbol{\alpha}(n-1), \tau(n-1), \mathbf{D})$ ; sample the parameters  $\boldsymbol{\alpha}(n) \sim P(\boldsymbol{\alpha}|\boldsymbol{\omega}(n), \mathbf{D})$  and  $\tau(n) \sim P(\tau|\boldsymbol{\omega}(n), \mathbf{D}) - \mathbf{IF} \boldsymbol{\omega}(n), \boldsymbol{\alpha}(n)$  and  $\tau(n)$  samples reach stationary states **End For** 

#### 2.2.3 Burn-in period

In practice, an initial set of samples (burn-in) are often discarded to avoid starting biases [20]. The period required for the Markov chain to reach its stationary state is called the burn-in period. The burn-in period is usually determined by plotting the Markov chain samples through time. Moreover, the samples within the burn-in period are discarded. In this paper, by plotting the Markov chain samples, the burn-in period is obtained by visual inspection.

#### 2.2.4 The stability of the method

The coefficient of determination ( $\mathbb{R}^2$ ) and mean percentage error (MPE) is used to evaluate the accuracy of the proposed method, which are obtained as below. Where ( $K_i$ )<sub>*i*</sub> is the *i*<sup>th</sup> simulated data, (( $K_i$ )<sub>prg</sub>)<sub>*i*</sub> is the *i*<sup>th</sup> predicted value. The best value for  $\mathbb{R}^2$  is 1.0, and the smaller the value of MPE, the better the predicted result.

$$\mathbf{R}^{2} = \left(\frac{n\sum \mu_{(K_{t})_{i}} \times (K_{t})_{i} - \sum \mu_{(K_{t})_{i}} \sum (K_{t})_{i}}{\sqrt{n\sum \mu_{(K_{t})_{i}}^{2} - \left(\sum \mu_{(K_{t})_{i}}\right)^{2}} \sqrt{n\sum (K_{t})_{i}^{2} - \left(\sum (K_{t})_{i}\right)^{2}}}\right)^{2}$$
(21)

$$MPE = \left(\frac{1}{n}\sum_{i=1}^{n} \left| (K_{t})_{i} - ((K_{t})_{pre})_{i} \right| / (K_{t})_{i} \right) \times 100\% \quad (22)$$

The procedure for a set of experiments is described below. Five pairs are randomly selected from the datasets as training samples, and the rest of the data pairs are testing sets. The predicted model of the stress concentration factor is obtained by the method mentioned in Eq. (20). Comparing the predicted stress concentration factor with the simulated value,  $\mbox{R}^2$  and MPE are calculated.

total of 1000 experiments are conducted. А The frequency histogram of MPE and  $R^2$  are plotted in Fig. 4 and Fig. 5, where "Mean" the mean value of 1000 represents experiments, and "SD" represents standard deviation. By the figures, for 1000 experiments, the mean value of MPE is 4.2%, and its standard is 0.05. deviation Meanwhile, for most experiments, the  $R^2$  is around 0.94, and the standard deviation is 0.004. MPE and R<sup>2</sup> remain within the error tolerance range, which indicates the excellent stability of the method.



Fig. 4. Mean percentage error (MPE) of 1000 experiments



Fig. 5. Coefficient of determination(R<sup>2</sup>) of 1000 experiments

#### 3. RESULTS AND DISCUSSION

Firstly, using the five data from datasets as training samples, the predicted model of stress concentration factor is obtained through the proposed method. The first 500 samples of 10,000 samples obtained by Gibbs sampling are discarded because of the burn-in period. Based on the remaining 9,500 samples, the predicted mean stress concentration factor is calculated from their means and standard deviations. The predicted formula between  $K_t$  and statistical roughness parameters of the surfaces is expressed as

$$K_{t} = 1 + 1.915 \left(\frac{R_{a}}{R_{y}}\right)^{-0.223} \left(\frac{R_{a}}{R_{z}}\right)^{0.122} \left(\frac{R_{a}}{\rho}\right)^{0.549}$$
(23)

To make the results more intuitive, each predicted  $K_t$  in the 41 datasets are compared with the simulated  $K_t$  in Fig. 6. It is showed by open circles from mean  $K_t$  and error bars for uncertainly in terms of  $K_t$ +1.96SD, where SD is the standard deviation of each predicted  $K_t$ , to show the ranges of data. Fig. 6 also includes the true 1:1 line for comparison. It shows that open circles fluctuate around the 1:1 line, and most samples have relative errors smaller than 10%, and all samples smaller than 20%. The maximum

error is found to be 15.4%, and the average error is 3.7%. For quantitative the predicted model,  $R^2$  and MPE between predicted and simulated  $K_t$  are calculated, obtained as  $R^2$ =0.95, MPE=3.76%. The large  $R^2$  and small MPE together indicate that the predicted model is reasonably accurate.

For comparison, Fig. 7 also includes the stress concentration factor predicted by the Neuber model and Arola- Ramulu model.  $K_t$  predicted by the proposed method is closer to the 1:1 line, which indicates our predicted values are more consistent with the simulated values than the other two models. The average error of these two models is 9.87% and 21.23%, while for the proposed method, the average error is 3.76%.

To verify the influence of the number of data pairs ( $n_s$ ) on estimation performance, the randomly 5, 15, 30 groups of datasets are selected as training samples to obtain the corresponding predicted expressions. The predicted  $K_t$  are compared with simulated  $K_t$ , as shown in Fig. 8. The values predicted by the three correlation expressions all fluctuate around the 1:1 line. Furthermore,  $R^2$  and MPE of three correlation expressions are plotted in Fig. 9.  $R^2$  and MPE are kept around 0.94 and 4%, respectively.



Fig. 6. Predicted versus simulated  $K_t$ 



Fig. 7. Estimation results of  $K_t$  by the proposed method, Neuber model and Arola- Ramulu model



Fig. 8. Predicted  $K_t$  obtained by different  $n_s$  ( $n_s$ =5, 15, 30) versus simulated  $K_t$ 



Fig. 9.  $R^2$  and MPE calculated by different  $n_s$  ( $n_s$ =5, 15, 30)

It indicates no significant effect on the predicted results with decreasing the number of training samples in the appropriate range. In other words, the estimated error of the proposed method is on the reasonable range when the number of data pairs decreases. The results demonstrate that the proposed method performs well under limited training sets.

The above analysis proved that the proposed method could efficiently obtain the stress concentration factor explicit and has better accuracy than the previous models. Moreover, this method is quite convenient to be conducted through only a few FEM simulations or tests for certain machining processes.

## 4. CONCLUSION

This article proposes a novel Bayesian learning to obtain correlation expression between the stress concentration factor and statistical roughness parameters. The training samples and testing samples are selected from the database, which is constructed by FEM simulations. Using the Bayesian learning with Gibbs sampler, the correlation expression between the stress concentration factor and statistical roughness parameters of the surfaces is estimated. The accurate correlation expression gives good agreements with direct FEM simulations, which demonstrates the feasibility of using the proposed method. Compared to other models, the proposed method has the advantages of high accuracy and broad adaptability. In conclusion, this work demonstrates the viability of using machine learning to predict the stress concentration factor. It provides a simple and efficient approach to obtain the predicted stress concentration factor for the rough surfaces under a specific type of processing.

## **COMPETING INTERESTS**

Author has declared that no competing interests exist.

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Peer-review history: The peer review history for this paper can be accessed here: https://www.sdiarticle5.com/review-history/78407